

HG15NDM

- Note : 1) All Question are Compulsory
 2) All Questions Carry Equal Marks
 3) Figures to the Right side Indicate Marks.

Q1.A) Attempt any 4 (each of 5 marks)

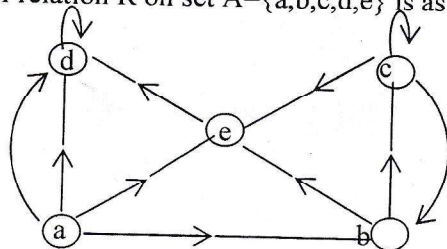
20M

- If $f: \mathbb{R} \rightarrow \mathbb{R}$ is defined by $f(x) = 2x+3$; then show that f is bijection & hence find f^{-1} .
- Let $f(x) = x^2 + 1$ & $g(x) = \frac{1}{x-1}$ then find $f \circ g(x)$.
- If the $f(x) = (2x-5)^{1/2}$ and $g(x) = 5x^2 - 3$ find the composite function by $f \circ g(x)$ & $G \circ f(x)$. verify whether $(f \circ g)(x) = (g \circ f)(x)$
- Determine whether each of these function is a bijective from \mathbb{R} to \mathbb{R}
 - $f(x) = 4-3x$
 - $f(x) = x^5+1$
 - $f(x) = (x+1)/(x+2)$
 - $f(x) = x$
- Verify whether the function $\delta: \mathbb{R} \rightarrow \mathbb{R}$ defined as $f(x) = 4x-1$ for all $X \in \mathbb{R}$ is
 - one-to-one
 - onto
- Determine whether each of these function form \mathbb{Z} to \mathbb{Z} is one to one
 - $F(n) = n-1$
 - $f(n) = n^2+1$
 - $f(n) = m^3$
 - $f(n) = (n/z)$

Q.2 Attempt any 4 (each of 5 marks)

20M

- Let $A = \{0,1,2,3,4\}$ let $R = \{ \langle 1,2 \rangle, \langle 1,3 \rangle, \langle 1,4 \rangle, \langle 2,3 \rangle, \langle 3,3 \rangle, \langle 4,2 \rangle \}$ & $\delta = \{ \langle 1,3 \rangle, \langle 2,2 \rangle, \langle 3,2 \rangle, \langle 4,2 \rangle \}$ find.
 - $R \circ (S \circ S)$
 - IS $R \circ S = S \circ R$?
- If $A = \{1,2,3\}$ & $R = \{(1,1), (1,2), (2,1), (2,2), (2,3), (3,1), (3,3)\}$ find $M(R)$ & $[M(R)]^2$
- If $A = \{1,2,3\}$ & $B = \{4,5,6\}$ and $R_1 = \{(1,1), (1,2), (2,2), (3,2), (3,3)\}$ & $R_2 = \{(4,4), (5,5), (6,6)\}$ find the matrix $m(R_1) \times m(R_2)$
- Let $A = \{1,2,3\}$ & R be a Relation on A defined by $xRY \iff X \leq Y$ find R and draw its diagram.
- The diagram of relation R on set $A = \{a,b,c,d,e\}$ is as follows.



Find relation R & also obtain matrix of R .

- Let $A = \{1,2,3,4,5,6\}$, Let $R = \{(a,b) \mid a \equiv b \pmod{2}\}$ is an equivalence relation?

Q-3. Attempt any 4 (each of 5 marks)

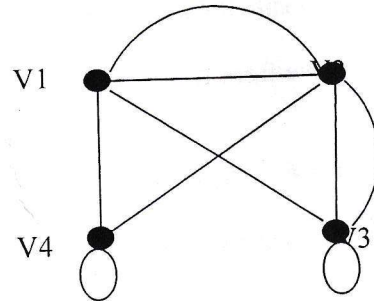
20M

- Let $f: A \rightarrow B$ and $A=B=\mathbb{R}$, $\delta(x) = X^4 + 1$ find f^{-1} .
- Let $R = \{(1,1), (1,3), (2,2), (2,4), (3,3), (3,1), (4,4), (4,2)\}$ be the relation on $A = \{1,2,3,4\}$ show that R is an equivalence relation on A . Also write down the equivalence classes with respect to relation R .
- Let R be a relation on \mathbb{Z} , defined by XRY is $5x+6y$ is divisible by 11 for $x,y \in \mathbb{Z}$ show that R is an equivalence relation on \mathbb{Z} .
- Let $A = \{1,2,3,4\}$ and $R = \{ \langle 1,2 \rangle, \langle 2,3 \rangle, \langle 3,4 \rangle \}$ find R^* transitive closure and draw its graph.
- For set $A = \{1,2,3,4,5\}$ the Relation matrix is

$$\begin{pmatrix} 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 0 \end{pmatrix} \text{ Draw its diagram.}$$

Q-4. Attempt any 4 (each of 5 marks)

- Let $A = \{1, 2, 3, 4, 12\}$ Let R be a partial order relation defined on A as $a R b$ if and only if a/b (a divides b) Draw the hasse diagram of partial order relation R .
- Find first six terms of the sequence defined by the following recurrence relation $a_n = a_{n-1} + 3 a_{n-2}$ with $a_0 = 1$ $a_1 = 2$
- Consider recurrence relation $a_n = a_{n-1} + 3 a_{n-2}$ with $a_9 = 2y, a_{10} = 12$ find y
- Find the adjacency matrix of following graph.



- Draw the graph represented by adjacency matrix.

$$\begin{array}{c}
 V1 \\
 V2 \\
 V3 \\
 V4
 \end{array}
 \begin{pmatrix}
 V1 & V2 & V3 & V4 \\
 0 & 2 & 1 & 1 \\
 2 & 0 & 2 & 1 \\
 1 & 2 & 1 & 0 \\
 1 & 1 & 0 & 1
 \end{pmatrix}$$

- Define the following graph with example
 - connected graph
 - Complete graph

***** BEST OF LUCK *****