(15M)

- 2) If $\int f(x) dx = 2 \int f(x) dx$ then f(x) is called as a) Even function

N.B.

- b) odd function
- c) constant function
- d) none of the above
- 3) A function is said to be invertible if and only if it is_ a)Bijective b) injective c) Inflexion d) Surjective
- $4) \lim_{x \to \infty} 1/3x =$ a)1 b)infinite c) zero d) None
- 5) A point on a curve where two curves crosses each other is called a)Cusps b) Asymptote c) Tangent d) Point of inflexion
- (b) Fill in the blanks:

(continuous, ∞, -∞, Modelling, ¼, ½, 5x+5y-8, axloga)

- 1. $\lim (-2x) = \underline{}$
- 2. The derivative of ax is ____
- is the process of writing a differential equation to describe a physical situation.

 $\pi_{/2}$ $\int \sin^3 x \cos x \, dx =$

5. Linearization of $x^3 + xy + y^2$ at (1, 2) is

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(c) Answer the following in one line

- 1. State $\in -\partial$ definition of limit
- 2. Define Concavity
- 3. Evaluate $\int [e^{2 \log x} + e^{x \log a}] dx$
- 4. Define the term Definite Integral
- 5. Define Absolute Extreme values

Q. 2 Attempt the following (Any THREE)

(15M)

- (a) Show that $\lim_{x \to 3} \frac{x^3 4x^2 + 13x 30}{x 3} = 16$
- (b) Show that |x| is continuous everywhere.
- (c) Find the intervals on which function $f(x)=x^2-4x+3$ is increasing or decreasing.
- (d) Find the relative extrema of $f(x) = 1 + 8x 3x^2$ using both first and second derivative test.
- (e) Using Newton's method find the approximate root for the equation $f(x)=x^3-x-1$
- (f) A garden is to be laid out in a rectangular area and protected by a chicken wire fence. What is the largest possible area of the garden if only 72 running feet of chicken wire is available for the fence?

Q. 3 Attempt the following (Any THREE)

(15M)

- (a) Evaluate $\int 1/(9\cos^2x + 4\sin^2x) dx$
- (b) Evaluate $\int_0^{\frac{\pi}{2}} \frac{1}{(1+cotx)} dx$
- (c) Solve the differential equation $(1 + y^2) dx + (1 + x^2) dy = 0$
- (d) Using Euler's method find approximate value of y when x = 1, in five steps, taking h = 0.2 for dy/dx = x + y and y(0) = 1.
- (e) Solve the differential equation $dy/dx + y tan x = cos^2x$
- (f) Evaluate $\int_{1}^{4} \sqrt{1+x^2} dx$ using simpson's rule with n=6

Q. 4 Attempt the following (Any THREE)

(15)

- (a) Find $\lim_{(x,y)\to(4,-2)} x(y^3+2x)^{\frac{1}{3}}$
- (b) Find the second order derivatives of $f(x,y)=y^2e^x+y$
- (c) If $z=x^2+y^2$, x=a cost and y=a sint. Use chain rule to find $\frac{dz}{dt}$.
- (d) Find the directional derivative of $f(x, y, z)=x^2y-yz^3+z$ at the point (1,-2,0) in the direction of the vector a = 2i + j 2k
- (e) Find the gradient vector of f(x, y) if $f(x, y) = x^3 + 2xy^2$. Evaluate it at (-3, -4)

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- (f) Find the equation for the tangent plane and parametric equations for normal line to the surface $z=x^2y$ at the point (2, 1, 4)
- Q. 5 Attempt the following (Any THREE)

(15)

- (a) Locate all relative extrema and saddle points of $f(x, y)=x^3+2y^3-3x^2-24y+16$
- (b) Solve the differential equation $x (x + y) dy y^2 dx = 0$
- Sketch the graph of the equation $y = x^3 + 5x + 7$ and identify the intervals where the function y is increasing and decreasing (draw the graph on the answer sheet itself).
- (d) $\pi_{/2}$ Evaluate $\int_{0}^{1} \sin 5x \cos 3x \ dx$
- (e) Find the asymptotes of the function $y = \frac{x}{(x+1)(x+2)^2}$
