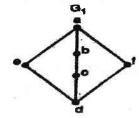
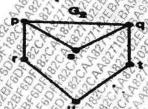
200	(2 ½ Hours)	Total Marks: 75]			
N.B.	1) All quanties are served.				
1V.D.	1) All questions are compulsory.	``````````````````````````````````````			
	2) Figures to the right indicate marks.				
	3) Illustrations, in-depth answers and diagrams will be appreci	ated, S. P. S. S. S. S.			
	4) Mixing of sub-questions is not allowed.				
020	ZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZZ	5 4 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5			
Q. 1	Attempt All (Each of 5Marks)	N 8 8 8 8 8 8 11			
- (a)	Select correct answer from the following:				
	 The product of two consecutive natural number is 	always divisible			
	by				
	(a) 3 (b) 2 (c) 6 (d) 10				
	2. The value of $P_3 = $	\$200,54 \$3000 B			
	(a) 35 (b) 210 (c) 30 (d) 71/3				
	3. A vertex with degree one is calledvertex.				
	(a) Pendant (b) isolated (c) incident (d) none	a of the shows			
	4. A graph with parallel edges and loops is called a	от це ароуе			
	(a) simple (b) pseudo (c) multiple (d) none of	grapa.			
	5. The out-degree of Sink 'z' of a Network is	x me above			
	(a) zero (b) No. of vertices (c) 1 (d) none of	\$\\$\			
	(a) and (b) two directices (c) (c) (d) none of	the above			
(b)	Fill in the blanks				
	(Coefficients, Chromatic, n, degree, equal, one)	180			
	THE APPLIES TO A SOLETA SERVICE AND	binomial			
	expansion.	DINOTHAL			
	$2^{-n}C_n = \underline{\qquad}$				
	3. The number of edges incident on a vertex is called of vertex				
40	4. William number of colours required to colour the vertices of the				
	graph is called number of the graph				
	5. In network the amount of flow leaving the source	is to the			
	amount of flow arriving at the sink.				
(A)	Short Answers				
₃ (c)					
	Second Principal of Mathematical Induction Binomial theorem				
	3. Labeled Tree				
	4. Planar graph				
	5. Flow 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5. 5.				
Q. 2	Attempt the following (Any THREE)	/15			
(a)	How many license plates can be made using either two letter	(15)			
	four digits or two digits followed by four letters?	as lonowed by			
(b)	Determine the coefficient on $x^2y^3z^2$ in the expansion of $(x + y + z)$	5 7			
(c)	For any positive integer n, the sum of squares of the first -				
	is $\frac{n(n+1)(2n+1)}{6}$, Prove by first principle of mathematical induction	ositive integers			
	6 7 1 10 to by thist principle of mathematical induction	on.			
the second secon	a company and a				

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- (d) How many integer-valued solutions are there for the equation $X_1 + x_2 + x_3 + x_4 + x_5 = 65$, all $x_i \ge 0$
- (e) What is Sudokt Puzzles? Write its benefits
- (f) For each n > 0, prove that $\binom{n}{0} \binom{n}{1} + \binom{n}{2} \dots + (-1)^n \binom{n}{n} = 0$
- Q. 3 Attempt the following (Any THREE)

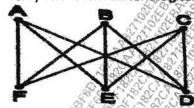
(a) Check whether the following graphs are isomorphic or not.





(15M)

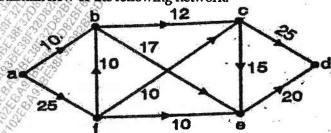
(b) Verify Euler's formula for the given connected graph.



- (c) What is bipartite graph? Show C₆(cycle of six vertices) is a bipartite graph.
- (d) State Ramsey's theorem for graphs and also estimate Ramsey Numbers R(2,4) and R(3,5)
- (e) Define adjacency matrix representation of a graph also draw the graph for

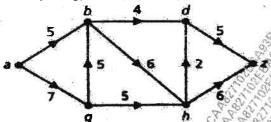
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are give	Colors	Cylhalix	0 0	1 0 1
S. C. 22 60		1888	lo o	0 1 1

- (f) Give an example of graph which is both Eulerian and Hamiltonian and justify it.
- Q. 4 Attempt the following (Any THREE) (15)
- a) Explain Polya's enumeration formula using chain index.
- (b) Explain Burnside's Lemma
- (c) Find maximum flow of the following network.



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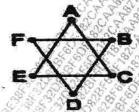
Define the capacity of cuts. Find the capacity of the cut (P,Q), (d) where $P=\{a, b, g\}$ and $Q=\{d, h, z\}$



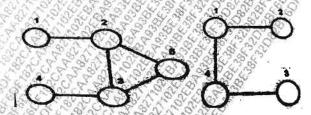
Write permutations shown below in cycle notation, compute $\pi_1\pi_2$ (product (e) of two permutations) and inverse of $\hat{\pi}_1$

 $\pi_1 = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 3 & 1 & 5 & 8 & 2 & 6 & 4 & 7 \end{pmatrix},$ $\pi_2 = \begin{pmatrix} 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 3 & 7 & 1 & 6 & 8 & 4 & 2 & 5 \end{pmatrix}$ Explain a Complete matching with example.

- (f)
- Q. 5 Attempt the following (Any THREE) (15)
- (a) In how many ways we can arrange the letters in the word MATHEMATICS?
- Find Chromatic number and Clique of the given graph. (b)



- (c) Explain the integer solutions of linear programming problems.
- (d) Determine the union and intersection of the graphs G1 and G2.



(e) Draw all regular graphs on 4 vertices with degree two.